# Best Time and Content for Delay Notification 

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#### Abstract

We consider an active information system, which aims to notify a traveler timely about a likely delay. Besides providing the right content, it should also wait for the best time for notification. This is especially true for mobile information services, where every notification may irritate the recipient.

We formulate and solve such a problem involving best choices both for content and time of notification by modeling it as an influence diagram. The chosen example stems from the domain of personal travel assistance.


Note that the action of the traveler is nothing else than a reaction to the notification from the information system.

## 1 Introduction

We aim to give a formal representation for a common but apparently not yet formalized decision problem. An information system (IS) providing timely notifications to a recipient faces the following task. Not only is it neccessary to decide on the best notification content at a given moment, but the IS must also decide whether to send the notification right away or to wait until later in order to decide on the notification content with improved precision. This is especially true for mobile or active decision support. Related work includes Mixed-Initiative-Assistance (cf. Ferguson et al. [5] and Horvitz [7]) and Just-In-Time-Information-Retrieval (JITIR) agents (cf. Rhodes [9]). A research project on information logistics at the FhG-ISST ${ }^{1}$ specifically addresses the aspect of timely notification.

We consider the domain of personal travel assistance.

[^0]Currently, the traveler consults an information system for the best route before he starts his journey and follows this route until he reaches his destination. However, delays may change the optimal route during the trip. This is especially true when parts of the routes are served by different transport providers, and connecting vehicles may not wait for a delayed passenger. Therefore, travelers must be informed about delays and alternative routes during their trip. The problem here is that delays are not certain in advance and early warnings could be misleading.

The following example will be studied in this article.
A traveler may reach his final destination on two distinct routes. The first route (by train) is considered to be faster than the second route (by taxi), but the latter is usually available without waiting, while the train may arrive late, causing the traveler to wait inefficiently.

The traveler has not yet decided which route to take, but will choose either of them with equal probability unless otherwise notified in time by the IS.

We will model the decision of the IS about time and content of the notification to be sent to the traveler. More specifically, we will decide whether to provide the best route now or to wait to provide a better route later.

The assumption here is that there is just one notification of the traveler. In other real-world problems, this constraint must be relaxed. In any case, extra notifications should be avoided.

## 2 Problem Formulation

Reasoning about the best time and content is a non-trivial task. The a-posteriori analysis may prove the a-priori decision to be ultimately wrong. In our example, the time of train departure influences the benefit of taking the train. A
notification supporting the traveler's decision for the right mode of transport should be sent before the train leaves the station.

Uncertainty will be modeled by probability theory, thus we employ random variables. The following points of time must be considered.

- $t_{\text {clock }}^{*}$, the current time or clock reading
- $t_{d}^{*}$, the real departure time of the train
- $t_{s}^{*}$, the scheduled time for the train departure
- $t_{m}^{*}$, the time of traveler notification

We intend to use time-dependent probabilities that do not refer to absolute times. Instead, these probabilities depend on the temporal distance from the scheduled time for the train departure. Therefore all time variables will be defined as follows.

- Clock $t_{\text {clock }}=t_{\text {clock }}^{*}-t_{s}^{*}$, the (relative) current time or clock reading
- Delay $t_{d}=t_{d}^{*}-t_{s}^{*}$, the (relative) departure time of the train
- Notification time $t_{m}=t_{m}^{*}-t_{s}^{*}$, the (relative) time of traveler notification

Beside continuous time variables the following discrete variables are needed (possible values are given in curly brackets):
$K(t)\{$ delay, unknown $\}$, the knowledge of the IS at time $t$ on the delay of the train. For $K(t)=$ delay, the train is known to be delayed, otherwise the IS has no knowledge about whether the train is delayed or not;

Weather $\{$ sunny, rainy $\}$, an external influence on the departure time. Weather serves as a representative example for other external influences as well;

Timely $\{y e s, n o\}$, denoting the timely or late arrival of the notification with the traveler. (only timely notifications are effective)

Content $\{$ take train,take taxi,none $\}$, the content of the notification to be sent to the traveler;

Action \{takes train,takes taxi\}, the action taken by the traveler.

The problem considered in this article can be stated now as follows. For each point in time $t \in \operatorname{dom}\left(t_{c l o c k}\right)$, the state space $S$ is the cross product $\operatorname{dom}(K(t)) \times \operatorname{dom}($ Weather $)$ and the decision space $D$ is the cross product $\operatorname{dom}\left(t_{m}\right) \times$ $\operatorname{dom}$ (Content). For a given state $s \in S$, the best decision $d \in D$ is the one with optimal expected reward. The influences between variables and reward are described below.

### 2.1 Reward based on Action and Delay

Both train delay and the action to be taken by the traveler influence the reward of the notification. The reward could, for instance, represent the likelihood of the traveler's arrival in time. In order to exclude trivial cases, we require the existence of two distinct train delays $t_{d}^{1}$ and $t_{d}^{2}$, such that different actions have to be taken by the traveler in order to maximize the reward, i.e.:
Reward(takes train, $\left.t_{d}^{1}\right)<$ Reward(takes taxi,,$\left._{d}^{1}\right) \wedge$
Reward (takes train, $\left.t_{d}^{2}\right)>$ Reward(takes taxi, $t_{d}^{2}$ )
This means, that there is no traveler action that dominates the other one for all possible delays $t_{d}$.

### 2.2 Delay influences Knowledge

The delay $t_{d}$ is related to the current knowledge $K(t)$ about this delay. The IS changes its knowledge due to external information processes which are not under consideration here. The following assumptions are made:

1. $K(t)$ is unknown until some point in time $t_{f}$ (flipping time), where it flips to delay. It never flips back.
2. If $K(t)$ flips to value delay, then the train must be delayed, i.e. $K(t)=$ delay is free of error.
3. If the train is delayed $\left(t_{d}>0\right)$, then flipping time $t_{f}$ and delay $t_{d}$ are independent, i.e. the delay does not influence the time the IS may learn about this delay.
$F(t)=P\left(t_{f} \leq t \mid t_{d}>0\right)$ is the distribution function of the flipping time $t_{f}$ (a random variable) given that $t_{d}>0$. $F(t)$ is the probability of $K(t)=$ delay given that the train is delayed $\left(t_{d}>0\right)$.

### 2.3 Action based on Timeliness and Content

As argued in the introduction, timeliness of notification may be influenced by many factors. Here we are primarily interested in the aspect of effectiveness, i.e. whether or not the action can be chosen after notification. There is a critical time after which notification becomes ineffective. In our setting, this would be the time when the traveler chooses between two alternative actions which exclusively lead either to takes train or takes taxi.

## 3 The Model

We model the decision problem with an influence diagram. Influence diagrams are directed graphs with three types of nodes (cf. Shachter [11] and Pearl [8]). Chance nodes (shown as ovals) represent uncertain quantities, decision nodes (shown as rectangles) represent possible decisions and value nodes (shown as diamonds) represent rewards and costs for decisions and outcomes of uncertain quantities. Directed links leading to chance nodes denote conditional dependency, directed links leading to value nodes denote functional dependency and directed links leading to decision nodes are informational, i.e. the respective quantity is known before the decision has to be made. For demonstration purposes, discrete points in time were used instead of continuous time.


Figure 1. The influence diagram

The influence diagram for the example is shown in figure 1. First, a short description of the nodes is given, including the variables which have been introduced before (cf. Section 2 for details).

## Chance Nodes:

Action $\{$ takes trainltakes taxi $\}$, the action of the traveler.
Weather $\{$ sunny/rainy\}, the external influence of the weather.

Timely $\{y e s / n o\}$, timeliness of notification is modeled by this chance node. Only timely information may influence the Action of the passenger. Timeliness is guaranteed for early information and impossible for late information. For timely information, timeliness is reached with high probability.
$K_{\text {clock }}\{$ delay/unknown $\}$, the IS knowledge at current (clock) time.
$K_{m}\{$ delay/unknown $\}$, the (expected) IS knowledge at notification time.
$t_{\text {clock }}\{-20 /-10 / 0\}$, the current clock time. The values may be interpreted as minutes.

Delay $\{$ in timeldelayed $\}$, the train delay. Delay $t_{d}$ has been replaced by this discrete two-valued variable ${ }^{2}$.

## Decision Nodes:

$t_{m}\{-20 /-10 / 0\}$, the time of notification.
Content $\{$ take trainltake taxi/none $\}$, the notification content.

## Value Nodes:

Reward, the reward given on timely arrival.
Penalty, a value node to ensure temporal consistency (see below).

The existence of most links follows directly from the discussion in Section 2.1-2.3 and will be continued in Section 3.1-3.4 for a concrete problem instance. The following comments consider the remaining issues.

Since we consider two different points in time, we also need to represent the IS knowledge for both points in time. $t_{\text {clock }}$ and $t_{m}$ can be viewed as parameters on the conditional distributions of $K_{\text {clock }}$ and $K_{m}$ (cf. Section 3.2). $K_{m}$ separates $K_{\text {clock }}$ from Delay, since $K(t)$ is free of error and independent of the delay.

Temporal consistency, i.e. $t_{c l o c k} \leq t_{m}$ is ensured by the Penalty-node. The penalty for $t_{c l o c k}>t_{m}$ is chosen to be greater than the absolute value of the maximum reward, i.e. for the maximum reward $R_{\max }$, penalty is $P=-\left(R_{\max }+\epsilon\right)$. For any choice of $t_{\text {clock }}$ and $t_{m}$, the expected value of Penalty is either $-\left(R_{\max }+\epsilon\right)$ or 0 . Therefore, the expected value of Reward + Penalty is less than or equal to $-\epsilon$ for choosing $t_{m}$ inconsistently and greater or equal to 0 for choosing $t_{m}$ consistently. Therefore, the consistent choice of $t_{m}$ will always be preferred versus the inconsistent choice of $t_{m}$.

The informational link between $K_{m}$ and Content is crucial as the content does not need to be determined before $t_{m}$ is reached and thus $K_{m}$ is known (and equal to $K_{\text {clock }}$ ).

The decisions on notification time $\left(t_{m}\right)$ and notification content (Content) are modeled as decision nodes, while the traveler's action (Action) is modeled as chance node. This is justified by the fact, that changes in the traveler's actions are only reactions to notifications stemming from the IS.

The joint distribution of all variables is given by the marginal distributions for clock $t_{\text {clock }}$ and Weather together with conditional probability tables for all other variables with respect to their predecessors. Instances of the problem are calculated by entering evidence for $t_{\text {clock }}, K_{\text {clock }}$

[^1]and Weather and propagating this information through the network until the new joint distribution is computed.

### 3.1 Reward based on Action and Delay

The reward is given in Table 1 below. For Action=takes taxi the reward is independent of the delay. 50 is the reward for taking the taxi. We can think of the reward as giving the likelihood of timely arrival at some destination (in percent). Then the values can be interpreted in the following manner:

- By taxi, the traveler will reach her destination in time with a likelihood of $50 \%$.
- By train, the traveler will reach her destination in time with a likelihood of $100 \%$, if the train is in time, and with $0 \%$, if the train is delayed.

| Action | takes train |  | takes taxi |  |
| :--- | :--- | :--- | :--- | :--- |
| Delay | in time | delayed | in time | delayed |
| Reward | 100 | 0 | 50 | 50 |

Table 1. Reward

### 3.2 Delay influences Knowledge $K(t)$

The relationship between the delay (Delay) and the imperfect knowledge $K(t)$ is shown in Table 2 for $K_{m}$ and in Table 3 for $K_{\text {clock }}$. In Table 2, the distribution of $K_{m}$ depending on the random variables Delay and $t_{m}$ is shown, while in Table 3 the distribution of $K_{\text {clock }}$ is shown depending on random variables $K_{m}, t_{m}$ and $t_{\text {clock }}$.

If Delay $=$ in time and $t_{m}=-20$, then $K_{m}=$ delay with a probability of $0 \%$ (cf. Table 2). If the train will be delayed (Delay $=$ delayed), then $K_{m}=$ delay with probabilities of $20 \%, 50 \%$ and $90 \%$ at $t_{m}$ equal to $-20,-10$ and 0 respectively.

For $K_{m}=$ unknown, $K_{\text {clock }}$ is unknown due to $K(t)$ being free of error. The last column of Table 3 represents this fact in a shorthand representation. For $t_{\text {clock }}=t_{m}$, also $K_{\text {clock }}=K_{m}$. Since $t_{\text {clock }}>t_{m}$ is formally not forbidden, we assume equivalence of $K_{m}$ and $K_{\text {clock }}$ in these unspecified cases. For $t_{\text {clock }}<t_{m}$, the conditional probabilities can be inferred from the distribution of the flipping time. The distribution function for the flipping time is implicitly given in Table 2 by $F(t)=P\left(K_{m}=\right.$ delay $\mid$ Delay $=$ delayed $\wedge t=$ $t_{m}$ ). The following values are known:
$F(-20)=0.2$
$F(-10)=0.5$
$F(-0)=0.9$
Hence the conditional probabilities can be calculated for Table 3 as well. As an example, we consider the probability
of $K_{\text {clock }}=$ delay for $K_{m}=$ delay, $t_{m}=-10$ and $t_{\text {clock }}=-20$. The probability is given by:
$P\left(K_{\text {clock }}=\right.$ delay $\mid K_{m}=$ delay $\left.\wedge t_{m}=-10 \wedge t_{\text {clock }}=-20\right)=$
$P(K(-20)=$ delay $\mid K(-10)=$ delay $)=$
$P(K(-20)=$ delay $\wedge K(-10)=$ delay $) \div P(K(-10)=$ delay $)=$ $F(-20) \div F(-10)=0.2 \div 0.5=0.4$

The value is underlined in the Table 3. The qualification on Delay $=$ delayed can be omitted here, as $K(t)=$ delay is sufficient for Delay=delayed.

|  | Delay | in time |  |  | delayed |  |  |
| :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: |
|  | $t_{m}$ | -20 | -10 | 0 | -20 | -10 | 0 |
| $K_{m}$ | delay | 0 | 0 | 0 | 0.20 | 0.5 | 0.9 |
|  | unknown | 1 | 1 | 1 | 0.80 | 0.5 | 0.10 |

Table 2. Knowledge $K_{m}$

|  | $K_{m}$ | delay |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | $t_{m}$ | -20 |  |  | -10 |  |  |
|  | $t_{\text {clock }}$ | -20 | -10 | 0 | -20 | -10 | 0 |
| $K_{\text {clock }}$ | delay | 1 | 1 | 1 | 0.40 | 1 | 1 |
|  | unknown | 0 | 0 | 0 | 0.60 | 0 | 0 |


|  | $K_{m}$ | delay |  |  | unknown |
| :--- | :--- | :---: | :---: | :---: | :---: |
|  | $t_{m}$ | 0 |  | $*$ |  |
|  | $t_{\text {clock }}$ | -20 | -10 | 0 | $*$ |
| $K_{\text {clock }}$ | delay | 0.22 | 0.56 | 1 | 0 |
|  | unknown | 0.78 | 0.44 | 0 | 1 |

Table 3. Knowledge $K_{\text {clock }}$
Temporal consistency $\left(t_{\text {clock }} \leq t_{m}\right)$ is enforced for the decision on $t_{m}$ by the Penalty-node (Table 4). The penalty for $t_{\text {clock }}>t_{m}$ is chosen to be -101 thus being absolutely greater than the maximum reward which is 100 .

| $t_{m}$ | -20 |  |  | -10 |  |  | 0 |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $t_{\text {clock }}$ | -20 | -10 | 0 | -20 | -10 | 0 | $*$ |
| Cost | 0 | -101 | -101 | 0 | 0 | -101 | 0 |

Table 4. Penalty

### 3.3 Action based on Timely and Content

Late notification results in failure to inform the traveler in time. This is represented by Timely (Table 5). Earliest notification $\left(t_{m}=-20\right)$ results in Timely $=y e s$, while late notification $\left(t_{m}=0\right)$ results in Timely=no. An intermediate notification time ( $t_{m}=-10$ ) will be timely with a probability of $90 \%$. The Action (Table 6) does not depend on the Content for Timely=no or Content=none. In these cases Action takes both values with equal probability.

|  | $t_{m}$ | -20 | -10 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| Timely | yes | 1 | 0.9 | 0 |
|  | $n o$ | 0 | 0.10 | 1 |

Table 5. Timely

|  | Timely | yes |  |  | no |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Content | take train | take taxi | none | $*$ |
| Action | takes train | 1 | 0 | 0.5 | 0.5 |
|  | takes taxi | 0 | 1 | 0.5 | 0.5 |

Table 6. Action

### 3.4 External factor Weather

The influence of the external factor Weather on the Delay is shown in Table 7.

|  | Weather | sunny | rainy |
| :--- | :--- | :--- | :--- |
| Delay | in time | 0.7 | 0.30 |
|  | delayed | 0.30 | 0.7 |

Table 7. Delay

### 3.5 Marginal Distributions

For completeness, the marginal distribution of Weather is given in Table 8 (left). $t_{\text {clock }}$ is given with an evidence (-10) in Table 8 (right). Since this is no distribution, $t_{\text {clock }}$ may also bear other evidences.

| Weather | sunny <br> rainy | 0.5 |
| :--- | :--- | :--- |


| $t_{\text {clock }}$ | -20 | 0 |
| :--- | :--- | :--- |
|  | -10 | 1 |
|  | 0 | 0 |

Table 8. Weather and clock $t_{\text {clock }}$

## 4 What-if Scenarios

Some scenarios will be presented in the following. The expected value of Reward + Penalty (also referred to as utility) will be denoted by $E$.

### 4.1 Scenario I(a): Weather $=$ sunny $/ t_{\text {clock }}=-20$

Evidence for Weather (sunny) is entered, clock time $t_{\text {clock }}$ is -20 and $K_{\text {clock }}$ is unknown. The resulting utilities for different decisions on notification time $t_{m}$ and Content are shown in Table 9 below.

| $t_{m}$ | E |
| :--- | :--- |
| -20 | 74.47 |
| -10 | 77.55 |
| 0 | 62.23 |


| Content | E |
| :--- | :--- |
| take train | 74.47 |
| take taxi | 62.23 |
| none | 62.23 |

## Table 9. Results for Scenario I(a)

The optimal notification time $t_{m}$ is -10 . Therefore, notification can be deferred. The optimal content (Content) cannot be determined, until notification time $t_{m}$ is fixed.

### 4.2 Scenario I(b): Weather $=$ sunny $/ t_{\text {clock }}=-10$

Now, clock time $t_{\text {clock }}$ is -10 and $K_{\text {clock }}$ is still unknown. Again, -10 is the optimal notification time (Table 10 (left)). Notification has to be made immediately. For immediate notification, the resulting utilities for different decisions on Content can be seen in Table 10 (right).

| $t_{m}$ | E |
| :--- | :--- |
| -20 | -26.53 |
| -10 | 80.74 |
| 0 | 66.18 |


| Content | E |
| :--- | :--- |
| take train | 80.74 |
| take taxi | 51.62 |
| none | 66.18 |

## Table 10. Results for Scenario l(b)

Obviously, the notification content take train should be delivered.

### 4.3 Scenario II: Weather $=$ rainy $/ t_{\text {clock }}=-20$

Evidence for Weather (rainy) is entered, clock time $t_{c l o c k}$ is -20 and $K_{\text {clock }}$ is unknown. The resulting utilities for different decisions on the notification time $t_{m}$ are shown in Table 11 (left). In this case, -20 is the optimal notification time, although the utility for $t_{m}=-10$ is also near-optimal. The utilities for notification time $t_{m}$ and Content are shown in Table 11 (right).

| $t_{m}$ | E |
| :--- | :--- |
| -20 | 50 |
| -10 | 49.24 |
| 0 | 42.44 |


| Content | E |
| :--- | :--- |
| take train | 42.44 |
| take taxi | 50 |
| none | 42.44 |

Table 11. Results for Scenario II
Obviously, the notification content take taxi should be delivered.

## 5 Related Work

Reasoning with imperfect information has led to the theory of POMDP (Partially Observable Markov Decision Processes, cf. Hauskrecht [6]). Our model differs from previous work in this area:

- The temporal distance between successive states is not fixed, but given by the time variables $t_{m}$ (notification time) and $t_{\text {clock }}$ (clock reading).
- The transition probabilities do not only depend on the temporal distance between successive states, but also on the relative distance from the scheduled time $t_{s}$.

The representation of time in Bayesian networks has led to various distinct approaches. Berzuini [3] introduced a network of dates in order to reason about the probabilistic nature of event occurrence times for medical applications. Temporal random variables and continuous time is used in this work.

Dean and Kanazawa [4] propose random variables for duration as a means to represent semi-Markov processes in probabilistic networks. Tawfik and Neufeld [12] employ Temporal Bayesian Networks (TBN) for the representation of probabilities as functions of time. Arroyo-Figueroa and Sucar [2] model event occurrence times as nodes with respect to time intervals as developed by Allen [1]. This last approach is actually very similar to Berzuini's approach, but it is restricted to a finite number of intervals for the occurrence time of events.

We employ temporal variables in a manner similar to the one found in Berzuini, and Arroyo-Figueroa and Sucar. However, we employ relative points in time in order to represent the influence of temporal distances on the conditional probabilities.

## 6 Conclusion

The presented model enables decisions on immediate vs. deferred notification. The expected improvement of information precision is traded off against the expected loss of effectiveness.

Further investigations are aimed at incorporating two or more traveler (re-)actions and allowing for additional notifications.

## Acknowledgment

This research was supported by the DFG (Deutsche Forschungsgemeinschaft), Berlin-Brandenburg Graduate School in Distributed Information Systems (DFG grant no. GRK 316).

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[^0]:    ${ }^{1}$ Fraunhofer Gesellschaft - Institut für Software- und Systemtechnik (Germany).

[^1]:    ${ }^{2}$ [10] gives a quantitative model for the train delay $t_{d}$ and provides a graphical model for stochastic reasoning there-about.

